

Figure 1: Reactivity as a proportion of the distance from lower bound to upper bound for the hierarchical interactions food web models:  $(\text{reactivity} - \text{l.b.})/(\text{u.b.} - \text{l.b.})$ . For discrete time systems,  $\text{l.b.} = \max\left(\ln\left(\frac{\|\mathbf{J}\|_F}{\sqrt{n}}\right), \ln(\max(|J_{ij}|))\right)$  and  $\text{u.b.} = \ln(\|\mathbf{J}\|_F)$  (eqs. 9, 11). For continuous time systems,  $\text{l.b.} = \text{Re}\lambda_1(\mathbf{J})$  and  $\text{u.b.} = \|\mathbf{J}\|_F$  (eqs. 8, 16). Maximum interaction strength  $g = 2$ . I use only 4 species, as finding stable systems with more than 4 species become computationally prohibitive when the food web is 100% connected.

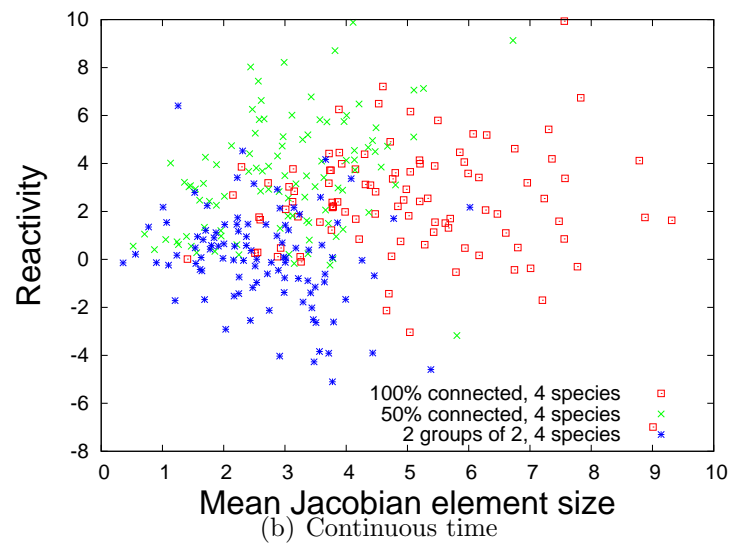
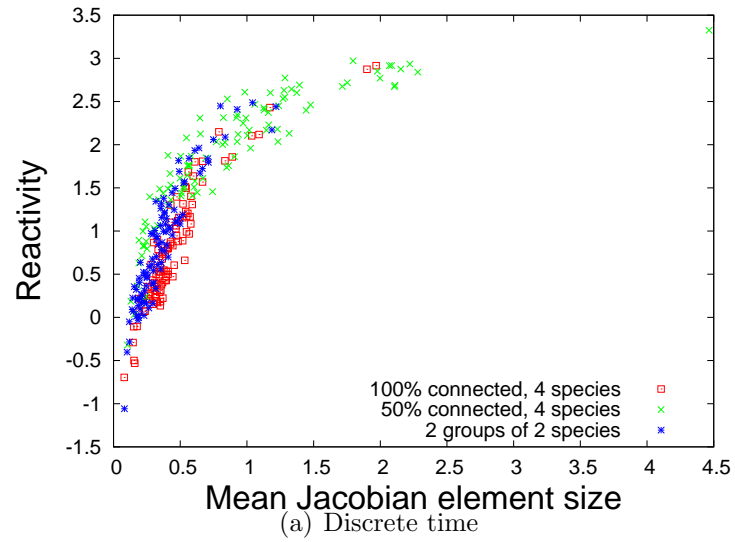


Figure 2: Reactivity vs mean Jacobian element size for the hierarchical interactions food web models,  $g = 2$ .