

# How far is the horizon?

## Geography and geometry

Elizabeth Meckes  
Case Western Reserve University

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### 1 The motivating question

How far away is the horizon?



*Elizabeth Meckes*

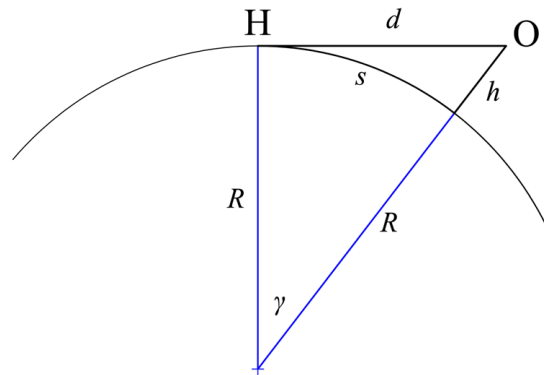
### 2 The model

To answer the question, we need a *mathematical model*: a simplified description and/or picture of the situation that lets us go from the question our eyes inspire to a question we can try to answer with calculations.

What picture to draw? What assumptions are we making? Do we believe them (completely, sort of, ...)?

### 3 Knowledge

Now that we have a model, what do we need to know in order to use it?

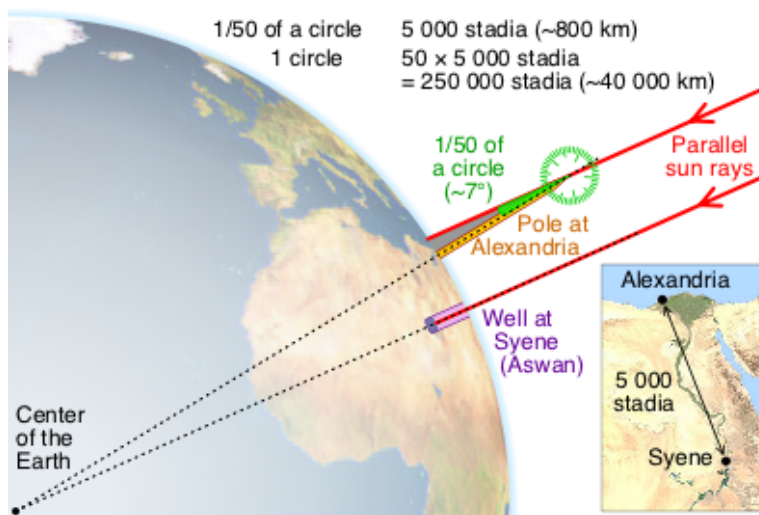


Jeff Conrad

The Pythagorean theorem:  $R^2 + d^2 = (R + h)^2$ .

## 4 Eratosthenes

Carl Sagan video.



cmglee, David Monniaux, jimht@shaw.ca

## 5 Turning things around

If you know  $d$  and  $h$ , you can find  $R$ .

Formula:

Then you could find the circumference of the earth:  $C = 2\pi R$ .

How might you figure out  $d$  without knowing  $R$ ?