

Let μ_1 and μ_2 be finite measures on (Ω, \mathcal{F}) ; for a signed measure ν , let $|\nu|$ denote the total variation (measure) of ν . Show that

$$|\mu_1 - \mu_2|(\Omega) = d_{TV}(\mu_1, \mu_2).$$