

1. Let $B(t)$ be Brownian motion and let

$$T := \inf\{t > 0 : B(t) < 0\}.$$

Find $\mathbb{E}[T]$.

2. Prove carefully that the probability that $B(t, \omega)$ is differentiable at $t = 0$ is zero.